

## Second Semester M.Tech. Degree Examination, Dec.08/Jan.09

### Finite Element Analysis

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions

- Explain the following with appropriate constitutive equations: i) Plane stress ii) Plane strain iii) Axisymmetry. (10 Marks)
  - Using Rayleigh Ritz method determine the deflection of a Cantilever beam at its free end carrying a point load  $P$  at its tip having a span of  $L$ . Use a suitable trial function having at least two Ritz constants. (10 Marks)
- Solve for stresses in the bar using principle of minimum potential energy. Refer figure Q2(a). (12 Marks)

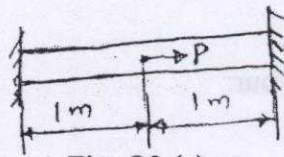


Fig. Q2 (a)

$$P = 2N$$

$$E = 1 \text{ N/m}^2$$

$$A = 1 \text{ m}^2$$

- Using two point formula, evaluate
  - $\int_{-1}^1 N d\xi$
  - $\int_{-1}^1 N^T N d\xi$
 where  $[N] = [N_1, N_2] = \left[ \frac{1-\xi}{2}, \frac{1+\xi}{2} \right]$ . (08 Marks)
- Derive an expression for  $[B]$  and  $[K]$  for 3 noded 1 D element with uniform cross sectional area. (12 Marks)
  - Discuss the penalty approach of handling boundary conditions. (08 Marks)
- Derive  $[J]$ ,  $[B]$  and  $[K]$  for CST element. (15 Marks)
  - Explain Galerkin's approach of solving engineering problems. (05 Marks)
- Evaluate the shape functions at point P given the coordinates as shown in figure Q5 (a). (10 Marks)

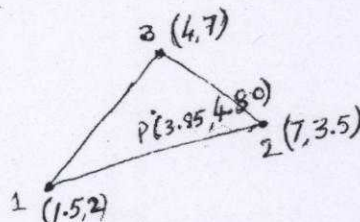
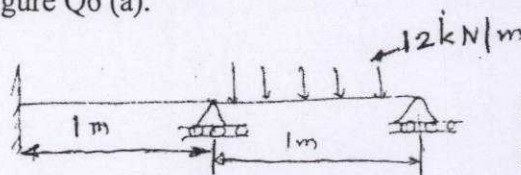


Fig. Q5 (a)

- Derive the shape functions of nine noded quadrilateral elements. (10 Marks)
- Determine the slopes at point 2 and 3 and also the deflection at centre of beam portion carrying UDL as shown in figure Q6 (a). (15 Marks)



$$E = 200 \text{ GPa}$$

$$I = 4 \times 10^6 \text{ mm}^4$$

Fig. Q6 (a)

- Sketch the shape function of 2 noded beam elements. (05 Marks)

7. a. Determine the temperature distribution in a composite wall as shown in figure Q7 (a). Use penalty approach of handling BCs. (16 Marks)

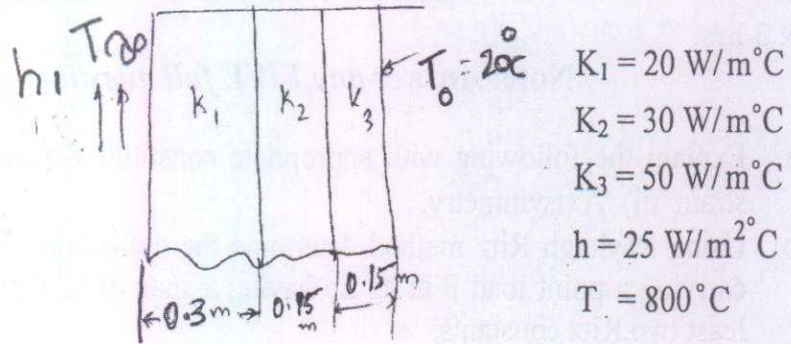


Fig. Q7 (a)

- b. Explain the boundary conditions as regards  $t_0$  solution in heat transfer problems by FEM. (04 Marks)

8 Write short notes on any four:

- Elemental mass matrix.
- Lumped mass.
- Convergence criteria.
- Truss element.
- Eigen values and vectors.

(20 Marks)

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